### September 2011

## MADALGO seminars by Moshe Lewenstein, Bar-Ilan University

#### Fast, precise and dynamic distance queries

#### Abstract:

We present an approximate distance oracle for a point set *S* with *n* points and doubling dimension  $\lambda$ .

For every  $\varepsilon > 0$ , the oracle supports  $(1 + \varepsilon)$ -approximate distance queries in (universal) constant time, occupies space  $[\varepsilon^{-0(\lambda)} + 2^{0(\lambda \log \lambda)}]n$ , and can be constructed in  $[2^{0(\lambda)} \log^3 n + \varepsilon^{-0(\lambda)} + 2^{0(\lambda \log \lambda)}]n$  expected time. This improves upon the best previously known constructions, presented by Har-Peled and Mendel. Furthermore, the oracle can be made fully dynamic with expected O(1) query time and only  $2^{0(\lambda)} \log n + \varepsilon^{-0(\lambda)} + 2^{0(\lambda \log \lambda)}$  update time. This is the first fully dynamic  $(1+\varepsilon)$ -distance oracle.

# Joint work with Yair Bartal, Lee-Ad Gottlieb, Tsvi Kopelowitz, Liam Roditty